# **Decoding**

Colin Cherry (Slides by Philipp Koehn)

MT Marathon 2012

# **Decoding**

• We have a mathematical model for translation

$$p(\mathbf{e}|\mathbf{f})$$

• Task of decoding: find the translation e<sub>best</sub> with highest probability

$$\mathbf{e}_{\mathsf{best}} = \mathsf{argmax}_{\mathbf{e}} \ p(\mathbf{e}|\mathbf{f})$$

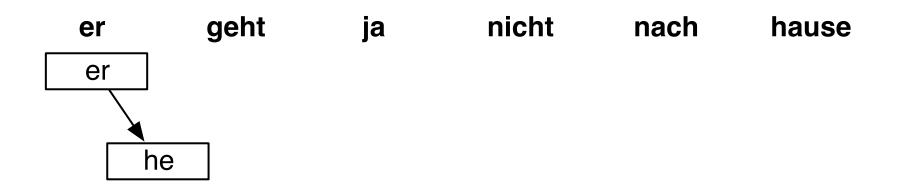
- Two types of error
  - the most probable translation is bad  $\rightarrow$  fix the model
  - search does not find the most probably translation  $\rightarrow$  fix the search
- Decoding is evaluated by search error, not quality of translations (although these are often correlated)

• Task: translate this sentence from German into English

er geht ja nicht nach hause

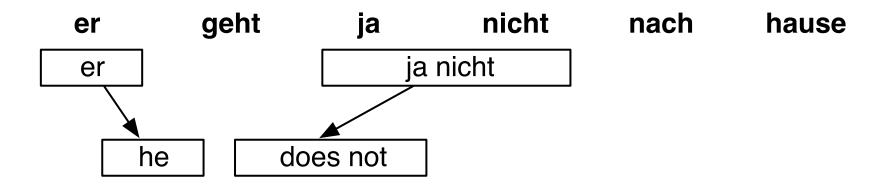
Decoding

• Task: translate this sentence from German into English



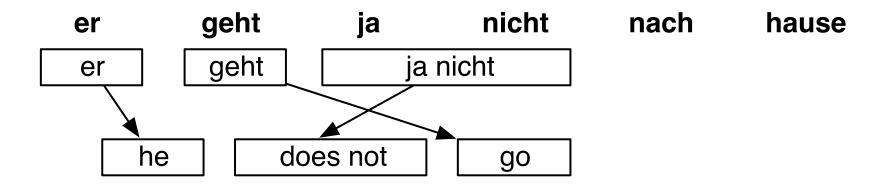
• Pick phrase in input, translate

• Task: translate this sentence from German into English



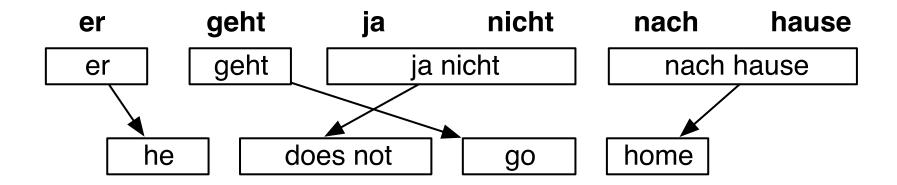
- Pick phrase in input, translate
  - it is allowed to pick words out of sequence reordering
  - phrases may have multiple words: many-to-many translation

• Task: translate this sentence from German into English



• Pick phrase in input, translate

• Task: translate this sentence from German into English



• Pick phrase in input, translate

### **Computing Translation Probability**

Probabilistic model for phrase-based translation:

$$\mathbf{e}_{\mathsf{best}} = \mathsf{argmax}_{\mathbf{e}} \ \prod_{i=1}^{I} \phi(\bar{f}_i|\bar{e}_i) \ d(start_i - end_{i-1} - 1) \ p_{\scriptscriptstyle \mathrm{LM}}(\mathbf{e})$$

- Score is computed incrementally for each partial hypothesis
- Components

**Phrase translation** Picking phrase  $\bar{f}_i$  to be translated as a phrase  $\bar{e}_i$ 

 $\rightarrow$  look up score  $\phi(\bar{f}_i|\bar{e}_i)$  from phrase translation table

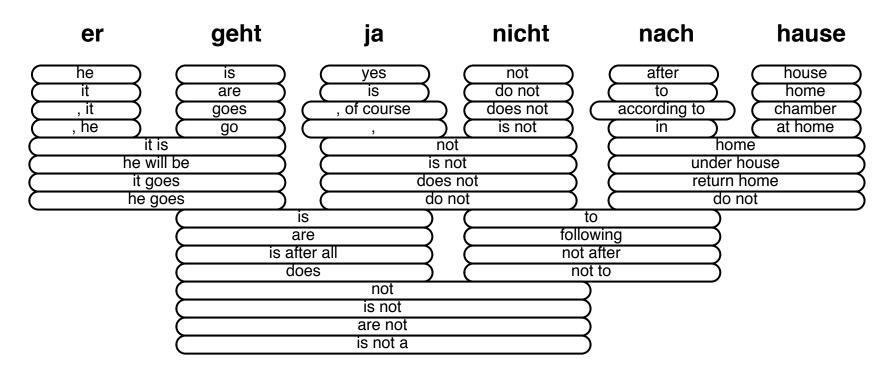
**Reordering** Previous phrase ended in  $end_{i-1}$ , current phrase starts at  $start_i$ 

 $\rightarrow$  compute  $d(start_i - end_{i-1} - 1)$ 

**Language model** For n-gram model, need to keep track of last n-1 words

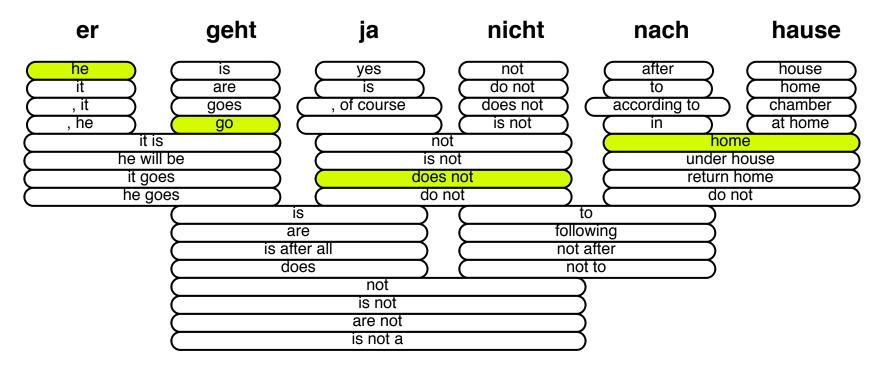
ightarrow compute score  $p_{\text{LM}}(w_i|w_{i-(n-1)},...,w_{i-1})$  for added words  $w_i$ 

### **Translation Options**



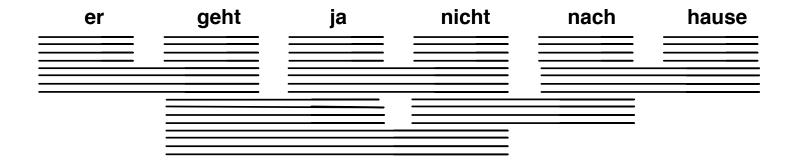
- Many translation options to choose from
  - in Europarl phrase table: 2727 matching phrase pairs for this sentence
  - by pruning to the top 20 per phrase, 202 translation options remain

### **Translation Options**



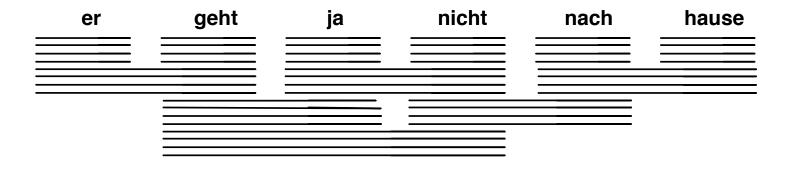
- The machine translation decoder does not know the right answer
  - picking the right translation options
  - arranging them in the right order
- → Search problem solved by heuristic beam search

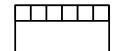
# **Decoding: Precompute Translation Options**



consult phrase translation table for all input phrases

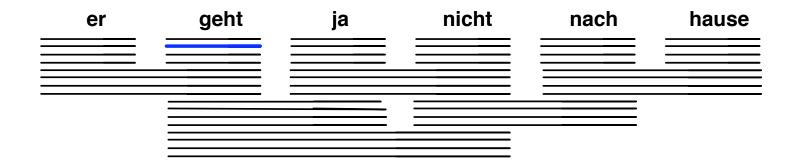
# **Decoding: Start with Initial Hypothesis**

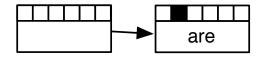




initial hypothesis: no input words covered, no output produced

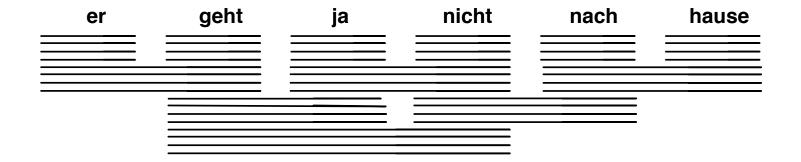
### **Decoding: Hypothesis Expansion**

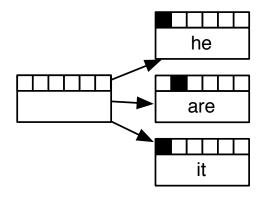




pick any translation option, create new hypothesis

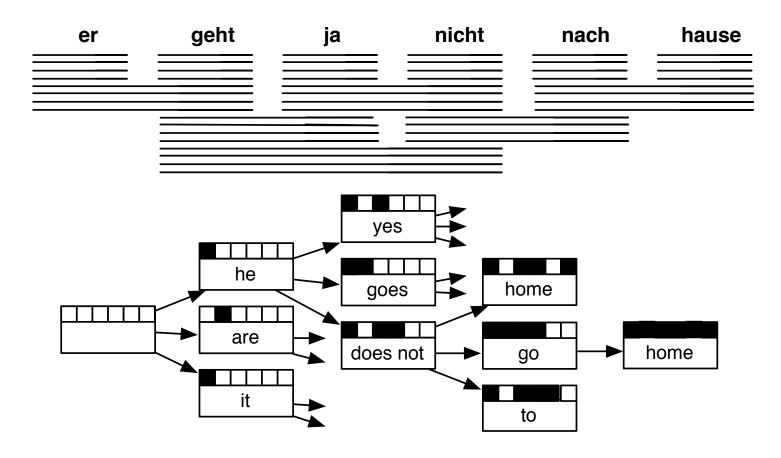
### **Decoding: Hypothesis Expansion**





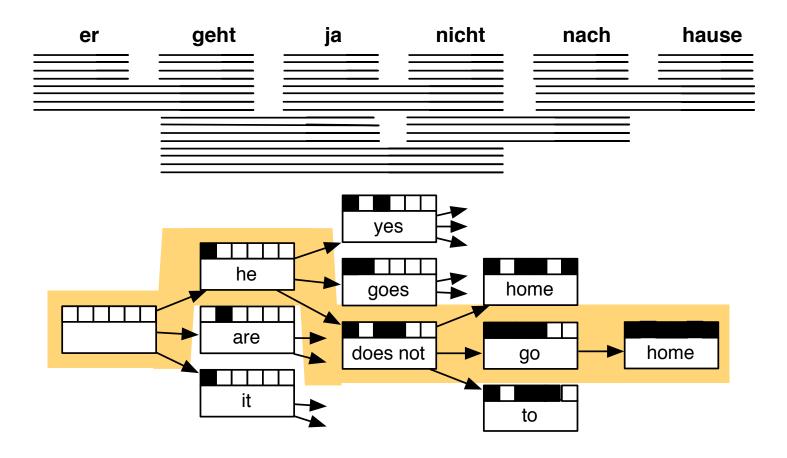
create hypotheses for all other translation options

### **Decoding: Hypothesis Expansion**



also create hypotheses from created partial hypothesis

# **Decoding: Find Best Path**



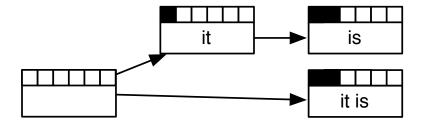
backtrack from highest scoring complete hypothesis

# **Computational Complexity**

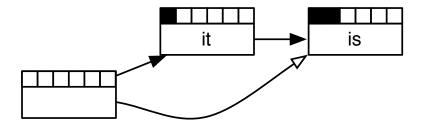
- The suggested process creates exponential number of hypothesis
- Machine translation decoding is NP-complete
- Reduction of search space:
  - recombination (risk-free)
  - pruning (risky)

### Recombination

- Two hypothesis paths lead to two matching hypotheses
  - same foreign words translated
  - same English words in the output
  - different scores

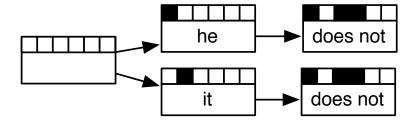


Worse hypothesis is dropped

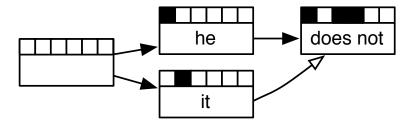


#### Recombination

- Two hypothesis paths lead to hypotheses indistinguishable in subsequent search
  - same foreign words translated
  - same last two English words in output (assuming trigram language model)
  - same last foreign word translated
  - different scores



Worse hypothesis is dropped



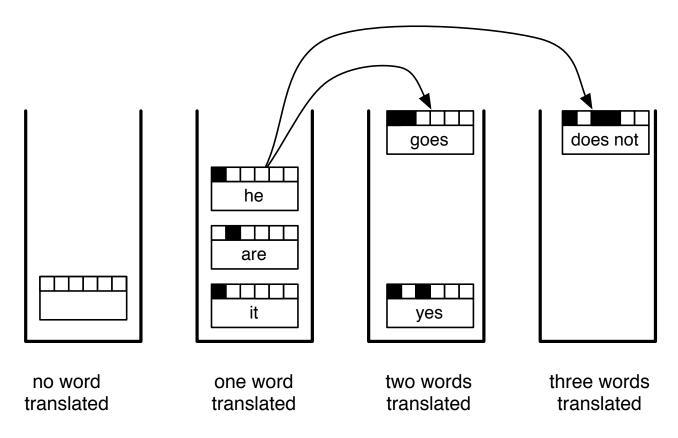
#### Restrictions on Recombination

- **Translation model:** Phrase translation independent from each other
  - → no restriction to hypothesis recombination
- Language model: Last n-1 words used as history in n-gram language model
  - $\rightarrow$  recombined hypotheses must match in their last n-1 words
- **Reordering model:** Distance-based reordering model based on distance to end position of previous input phrase
  - → recombined hypotheses must have that same end position
- Other feature function may introduce additional restrictions

### **Pruning**

- Recombination reduces search space, but not enough (we still have a NP complete problem on our hands)
- Pruning: remove bad hypotheses early
  - put comparable hypothesis into stacks
     (hypotheses that have translated same number of input words)
  - limit number of hypotheses in each stack

#### **Stacks**



- Hypothesis expansion in a stack decoder
  - translation option is applied to hypothesis
  - new hypothesis is dropped into a stack further down

### **Stack Decoding Algorithm**

```
1: place empty hypothesis into stack 0
2: for all stacks 0...n-1 do
     for all hypotheses in stack do
3:
        for all translation options do
4:
           if applicable then
5:
             create new hypothesis
6:
             place in stack
7:
             recombine with existing hypothesis if possible
8:
             prune stack if too big
9:
          end if
10:
        end for
11:
     end for
12:
13: end for
```

Decoding

# **Pruning**

- Pruning strategies
  - histogram pruning: keep at most k hypotheses in each stack
  - stack pruning: keep hypothesis with score  $\alpha \times$  best score ( $\alpha < 1$ )
- Computational time complexity of decoding with histogram pruning

 $O(\max \text{ stack size} \times \text{translation options} \times \text{sentence length})$ 

• Number of translation options is linear with sentence length, hence:

$$O(\max \text{ stack size} \times \text{ sentence length}^2)$$

Quadratic complexity

# **Reordering Limits**

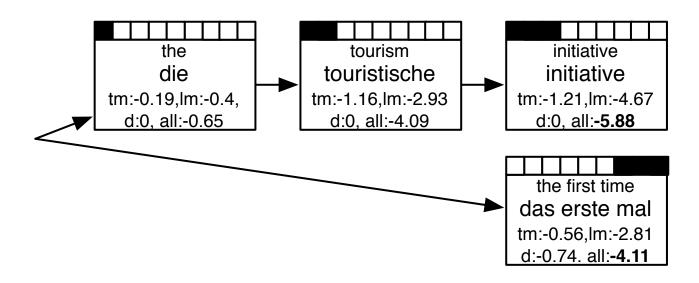
- Limiting reordering to maximum reordering distance
- Typical reordering distance 5–8 words
  - depending on language pair
  - larger reordering limit hurts translation quality
- Reduces complexity to linear

 $O(\max \text{ stack size} \times \text{ sentence length})$ 

Speed / quality trade-off by setting maximum stack size

### Translating the Easy Part First?

#### the tourism initiative addresses this for the first time



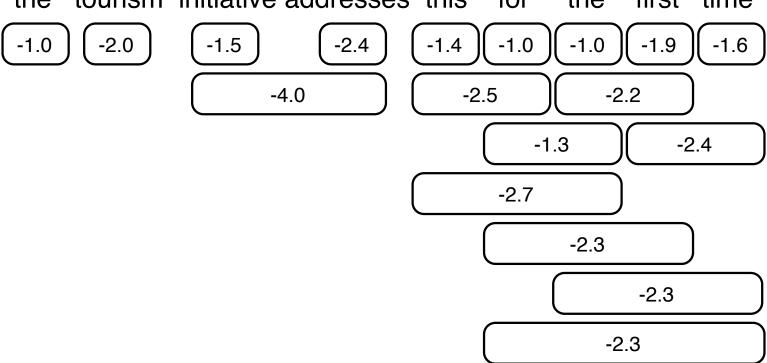
both hypotheses translate 3 words worse hypothesis has better score

### **Estimating Future Cost**

- Future cost estimate: how expensive is translation of rest of sentence?
- Optimistic: choose cheapest translation options
- Cost for each translation option
  - translation model: cost known
  - language model: output words known, but not context
    - → estimate without context
  - reordering model: optimistic estimate available
    - → (may not correspond to optimistic translation model's choices)

### **Cost Estimates from Translation Options**

the tourism initiative addresses this for the first time



cost of cheapest translation options for each input span (log-probabilities)

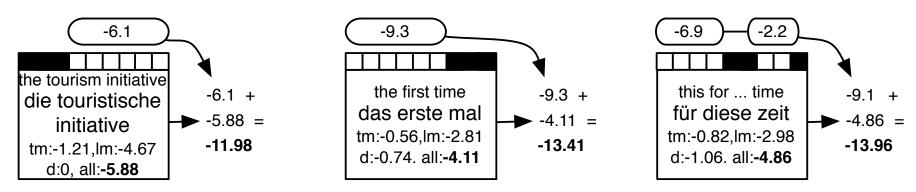
### **Cost Estimates for all Spans**

• Compute cost estimate for all contiguous spans by combining cheapest options

first	future cost estimate for $n$ words (from first)								
word	1	2	3	4	5	6	7	8	9
the	-1.0	-3.0	-4.5	-6.9	-8.3	-9.3	-9.6	-10.6	-10.6
tourism	-2.0	-3.5	-5.9	-7.3	-8.3	-8.6	-9.6	-9.6	
initiative	-1.5	-3.9	-5.3	-6.3	-6.6	-7.6	-7.6		•
addresses	-2.4	-3.8	-4.8	-5.1	-6.1	-6.1		•	
this	-1.4	-2.4	-2.7	-3.7	-3.7		-		
for	-1.0	-1.3	-2.3	-2.3		-			
the	-1.0	-2.2	-2.3		•				
first	-1.9	-2.4		-					
time	-1.6		•						

- Function words cheaper (the: -1.0) than content words (tourism -2.0)
- Common phrases cheaper (for the first time: -2.3) than unusual ones (tourism initiative addresses: -5.9)

# **Combining Score and Future Cost**

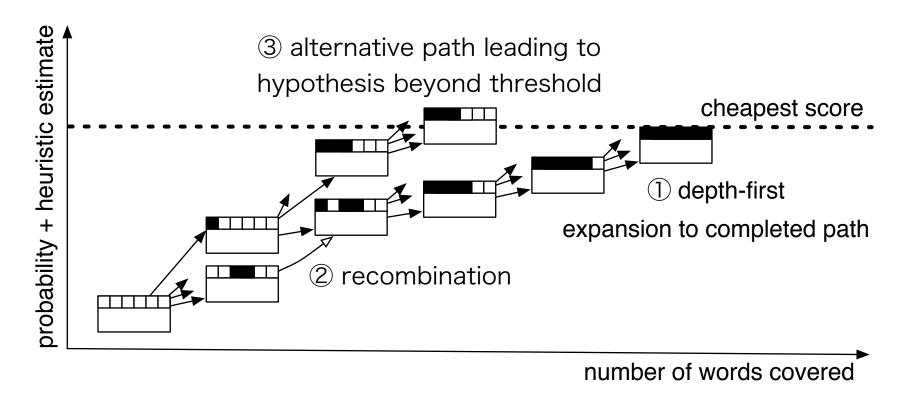


- Hypothesis score and future cost estimate are combined for pruning
  - left hypothesis starts with hard part: the tourism initiative score: -5.88, future cost: -6.1  $\rightarrow$  total cost -11.98
  - middle hypothesis starts with easiest part: the first time score: -4.11, future cost:  $-9.3 \rightarrow \text{total cost } -13.41$
  - right hypothesis picks easy parts: this for ... time score: -4.86, future cost:  $-9.1 \rightarrow \text{total cost } -13.96$

# **Other Decoding Algorithms**

- A\* search
- Greedy hill-climbing
- Using finite state transducers (standard toolkits)

### A\* Search



- Uses admissible future cost heuristic: never overestimates cost
- Translation agenda: create hypothesis with lowest score + heuristic cost
- Done, when complete hypothesis created

# **Greedy Hill-Climbing**

- Create one complete hypothesis with depth-first search (or other means)
- Search for better hypotheses by applying change operators
  - change the translation of a word or phrase
  - combine the translation of two words into a phrase
  - split up the translation of a phrase into two smaller phrase translations
  - move parts of the output into a different position
  - swap parts of the output with the output at a different part of the sentence
- Terminates if no operator application produces a better translation

### **Summary**

- Translation process: produce output left to right
- Translation options
- Decoding by hypothesis expansion
- Reducing search space
  - recombination
  - pruning (requires future cost estimate)
- Other decoding algorithms